

FASTER CARRY-PROPAGATE ADDERS

Faster Carry-Propagate Adders

- The entire goal to make faster adders is to resolve the carry across the entire adder structure more quickly
- It should be perplexing at first glance how this could be possible given the dependence of *every* output bit on the *LSB input bits*
- A few common faster CPAs:
 - 1) Carry Select
 - Speculatively add and select later
 - 2) Carry Lookahead
 - Look at how a carry propagates through a group of bits
 - 3) Conditional-sum (recursive carry select)
 - 4) Carry skip
 - 5) Other parallel prefix adders
 - Kogge-Stone, 1973
 - Brent-Kung, 1982
 - etc.

1) Carry Select Adder

- Break ripple adder into pieces
- Compute each sub-block (except the one covering the least-significant bits) twice: once assuming the carry input is a “0” and once assuming the input is a “1”
- Each sub-block computes 1) sum bits and 2) a single carry bit
- A mux selects correct sum+carry bits when the previous block’s carry-out (the carry-in of the block containing the mux) is known
- This method can be sped up further with a hierarchical structure (conditional-sum)

2) Carry Lookahead Adder

- Break ripple adder into pieces
- Look at the bits inside of each piece and decide two things *based only on the input operands and independent of the sub-block's carry-in*
 - Will this sub-block generate a carry-out regardless of the carry-in (*generate*)
 - Will the carry-out be equal to the value of the carry-in (*propagate*)
 - Other variations include a condition to stop a carry (*kill*)
- In the simplest form, the carry-out can be calculated by,
$$c_{out} = \text{Generate OR (Propagate AND } c_{in})$$
- Key point: Each sub-block pre-examines the input operand bits and gets ready for fast carry-out calculation
- There are a number of more complicated variations
- This method can be sped up further with a hierarchical structure

2) Carry Lookahead Adder

- When is Generate = 1?
 - When $c_{in} = 0$ and $c_{out} = 1$
 - When $a + b = \{c_{out}, \text{sum}\} = \{1xxx\dots xxx\}$ with $c_{in} = 0$
 - For example, $a[3:0] + b[3:0] = 1xxxx$ with $c_{in} = 0$
 - It will be true that Generate = 1 when $c_{in} = 1$ and $c_{out} = 1$, but that is not sufficient to show the cases when Generate = 1
- When is Propagate = 1?
 - When $a + b = \{c_{out}, \text{sum}\} = \{0111\dots 111\}$
 - For example, $a[3:0] + b[3:0] = 01111$